

CFD Study on Local Fluid-to-Wall Heat Transfer in Packed Beds and Field Synergy Analysis

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To reach the target of smaller pressure drop and better heat transfer performance, packed beds with small tube-to-particle diameter ratio ($D/d_p < 10$) have now been considered in many areas. Fluid-to-wall heat transfer coefficient is an important factor determining the performance of this type of beds. In this work, local fluid-to-wall heat transfer characteristic in packed beds was studied by Computational Fluid Dynamics (CFD) at different Reynolds number for $D/d_p = 1.5, 3.0$ and 5.6 . The results show that the fluid-to-wall heat transfer coefficient is oscillating along the bed with small tube-to-particle diameter ratio. Moreover, this phenomenon was explained by field synergy principle in detail. Two arrangement structures of particles in packed beds were recommended based on the synergy characteristic between flow and temperature fields. This study provides a new local understanding of fluid-to-wall heat transfer in packed beds with small tube-to-particle diameter ratio.

Keywords: Packed bed, Fluid-to-wall heat transfer, Field synergy principle, Computational fluid dynamics, Heat transfer intensification

Introduction

Packed beds have been extensively applied to chemical and industrial processes such as reactors, separators, dryers, filters and heat exchangers. To reach the target of smaller pressure drop and better heat transfer performance, packed beds are now being developed into small tube-to-particle diameter ratio ($D/d_p < 10$) (Dixon et al. [1]). Flow and heat transfer in this type of packed bed play an important role in determining the performance of the bed, and have therefore attracted an ever increasing attention of numerous investigations. A good local qualitative understanding and description of flow and heat transfer are important for the design and operation of such type of packed bed.

For heat transfer in packed beds, studies on fluid-to-wall heat transfer in packed beds could be classified as theoretical study, experimental research and numerical simulation. In theoretical studies, packed beds are generally treated as one-dimensional pseudo-homogeneous media, two-dimensional pseudo-homogeneous media and heterogeneous media. Then fluid-to-wall heat transfer coefficient is obtained as a part of governing equation or a boundary condition. Hsu and Cheng [2] and Ozgumus et al. [3] had made a perfect summarization on two-dimensional pseudo-homogeneous model in packed beds. The one-dimensional pseudo-homogeneous model now could be easily solved out. And, the analytical solutions for two-dimensional pseudo-homogeneous model and heterogeneous model were also presented by Dixon and

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Nomenclature A_i sectional area of an element (m^2) d_p diameter of particle (m) D diameter of the packed bed (m) h_z local fluid-to-wall heat transfer coefficient ($\text{W}/(\text{m}^2 \text{K})$) $\Delta p/L$ Pressure drop per unit length (Pa/m) Pr Prandtl number $q_w|_z$ local heat transfer in the wall (W/m^2) r radial position (m) Re_z Reynolds number based on superficial velocity Re_ϵ Reynolds number based on interstitial velocity $T_{f,ave}|_z$ local average temperature of fluid (K) T_w Wall temperature (K) ΔT Temperature gradient (K/m) U fluid velocity in the entrance of packed beds (m s^{-1}) V_{dz} volume of the macro-cylinder with the length of dz $V_{p,dz}$ volume of particles in the macro-cylinder with the length of dz x position in x direction (m) y position in y direction (m) z axial position (m)**Greek Symbols** ϵ average void fraction through the bed ϵ_z void fraction in the infinitesimal cylinder between z and $z+dz$ θ_i synergy angle in a mesh element in the x - y plane $\theta_{ave,z}$ average synergy angle in the x - y plane

Cresswell [4]. However, the local information about fluid-to-wall heat transfer is all absent in theoretical studies.

Experimental studies on fluid-to-wall heat transfer in packed beds mostly focus on developing an explicit correlation of fluid-to-wall heat transfer coefficient to predict its value. Several correlations for fluid-to-wall heat transfer coefficient in packed beds can be found in the literatures. Both Miroliaei et al. [5] and Jorge et al. [6] had made a summarization on correlations for fluid-to-wall heat transfer coefficient in packed beds. Wen and Ding [7] also summarized correlations of fluid-to-wall heat transfer coefficient in packed beds and concluded that the Li-Finlayson correlation agrees best with their experimental data. However, the effect of local structure on fluid-to-wall heat transfer is not easy to be obtained in experimental studies.

Computational Fluid Dynamics (CFD) is extensively used to investigate the fluid-to-wall heat transfer due to the fact that it is an effective tool for gaining local details in packed beds. Nijemeisland and Dixon [8] simulated fluid-to-wall heat transfer in packed beds by CFD, the results of which are in good agreement with the correlations proposed in the literatures. Guardo et al. [9] investigated the influence of turbulence model in CFD modeling on wall-to-fluid heat transfer in packed beds. Logtenberg and Dixon [10] also used computational fluid dynamics to obtain the values of the dimensionless wall heat transfer coefficient. Unfortunately, to the best of our knowledge, how the local packing and flow structure are related to fluid-to-wall heat transfer in packed beds and what packing structures are optimal for heat transfer enhancement are still questions in the literatures.

To address the above issues, the aim of this work is to establish a relation between local structure and fluid-to-wall heat transfer in packed beds with small tube-to-particle diameter ratio. We first use the Discrete Element Method (DEM) to obtain three-dimensional packed beds randomly packed with spherical particles in a cylindrical tube. Then the flow and local fluid-to-wall heat transfer in the beds are simulated by CFD. Finally, field synergy principle is used to analyze the effect of local packing and flow structure on fluid-to-wall heat transfer in packed beds, and the optimized structures are given.

Numerical methodology**Governing equations**

For the simulations in this study, full three-dimensional governing equations were applied. The conservation of mass, momentum and energy are needed for the flow and heat transfer of single phase fluid.

The continuity equation for conservation of mass is given as:

$$\frac{\partial}{\partial x_i}(\rho u_i) = 0 \quad (1)$$

where ρ is the mass density, x_i are the Cartesian coordinates, and u_i are the velocity components.

The momentum equation for conservation of momentum is given as:

$$\frac{\partial}{\partial x_j}(\rho u_i u_j) = -\frac{\partial p}{\partial x_i} + \frac{\partial \tau_{ij}}{\partial x_j} + \rho g_i \quad (2)$$

where p is the static pressure, g_i is the gravitational body force, τ_{ij} is the stress tensor, defined as follows for

Newtonian fluid:

$$\tau_{ij} = \left[\mu \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \right] - \frac{2}{3} \mu \frac{\partial u_i}{\partial x_i} \delta_{ij} \quad (3)$$

where μ is the dynamic viscosity, and δ_{ij} is the Kronecker delta.

The energy equation for conservation of energy is given as:

$$\frac{\partial}{\partial x_i} (\rho u_i h) = \frac{\partial}{\partial x_i} \left(k_f \frac{\partial T}{\partial x_i} \right) + \frac{\partial}{\partial x_i} (u_j \tau_{ij}) \quad (4)$$

where h is the specific enthalpy, and k_f is the thermal conductivity.

For turbulent flow, as Guardo et al. [9], one-equation model is chosen for simulations on turbulent flow and its equation is as follows:

$$\rho u_j \frac{\partial k}{\partial x_j} = \frac{\partial}{\partial x_j} \left[\left(\mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] + \mu_t \frac{\partial u_j}{\partial x_i} \left(\frac{\partial u_j}{\partial x_i} + \frac{\partial u_i}{\partial x_j} \right) - c_D \rho \frac{k^{3/2}}{l} \quad (5)$$

where σ_k is Prandtl number of turbulence pulsation kinetic-energy, c_D is empirical coefficient, and μ_t is turbulent pulsating viscosity, defined as follows:

$$\mu_t = c'_\mu \rho k^{1/2} l \quad (6)$$

where c'_μ is empirical coefficient, and l is the turbulent pulsation length.

Geometric Model

The packing structure has an important influence on the flow and heat transfer characteristics in packed beds. Therefore, the establishment of it should approach to the real situation as far as possible. This study developed a three-dimensional packed bed structure with uniform spherical particles randomly packing in a cylindrical tube using Hertz-Mindlin non-linear contact model in Discrete Element Method (Ucgul et al. [11]). The packed beds with D/d_p of 1.5, 3.0 and 5.6 are shown in Fig. 1. In the simulations, the diameter of particles is 3mm and the length of the cylindrical tube is about five times the diameter of particles. Although the length of the beds is short, the entrance effect only affects magnitude of heat transfer and not impacts the morphological characteristics of heat transfer. The material of spherical particles is glass and that of tube wall is steel. As to coordinate system of the bed, the z direction is parallel to the axis of the bed, with the x and y directions determined by right-hand screw rule. For the bed with $D/d_p=5.6$, local void fraction of DEM simulation were compared with MRI data of Sederman et al. [12] and predicted values of correlations of Klerk [13] and Mueller [14], as shown in Fig. 2. It can be seen that the distribution of void fraction along the radial direction of the bed from simulation are, as a

whole, in agreement with MRI data and predicted values of correlations, though there are a little discrepancies between simulation and data/correlation, especially at the maxima and minima. Local void fraction of the simulation is slightly greater than experimental data because the simulated bed is loose packing compared with the experimental packing. Even so, the packing structure built using DEM could reflect the real situation of packed beds, considering the deviation of experiment and simulation and the change of real height of packed particles in the radial direction of the bed.

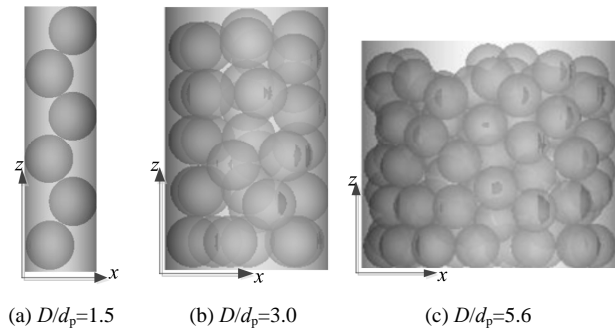


Fig. 1 Geometry models of packed beds with tube-to-particle diameter ratio of 1.5, 3.0 and 5.6.

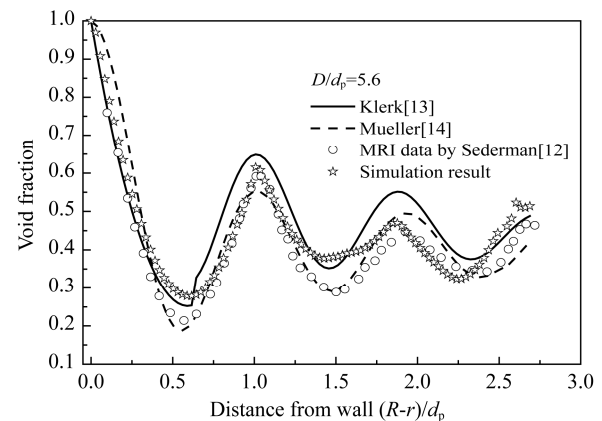


Fig. 2 Comparisons of radial distribution of void fraction between CFD calculation and MRI measurement and prediction of correlations in the packed bed with $D/d_p=5.6$.

Mesh generation

Before mesh generation, the zones near contact points of particle-particle and particle-wall must be modified for the good mesh quality and the calculating convergence in numerical simulations. In this work, particles were contracted by 0.5% of their diameter. As to this method, Dixon et al. [1] and Nijemeisland and Dixon [8] had made a conclusion that both the 99.5% and 99% sphere size models show negligible difference from the touching model in aspect of velocity distribution. Triangular mesh was chosen for the surface of particles and tube wall and tetrahedral mesh for fluid zone, as shown in Fig. 3. The

suitability of mesh used for the simulation is checked and the packed bed with $D/d_p=1.5$ is selected for mesh-independence verification. Three sets of meshes with total element number of 1683408, 3217115 and 7132803 are used for the test and the maximal mesh sizes in the fluid zone are of $d_p/10$, $d_p/20$ and $d_p/40$ correspondingly. Furthermore, the maximal mesh size on the particle surfaces is limited to $d_p/30$. It is shown in Fig. 4 that the deviation of velocity magnitude in meshes with the maximum mesh sizes of $d_p/10$ in fluid zone is very small with that of other two meshes. The mesh with the maximum size of $d_p/10$ in fluid zone is chosen for all packed beds, in order to avoid the big computer hardware requirements and shorten the calculation time.

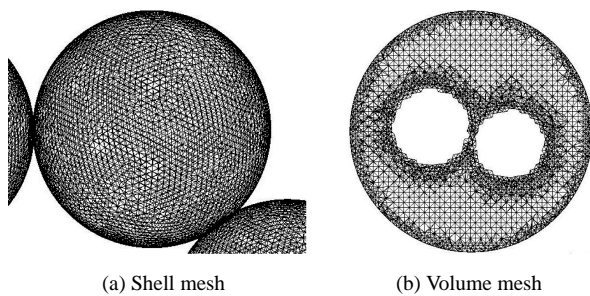


Fig. 3 Meshes in the packed bed with $D/d_p=1.5$.

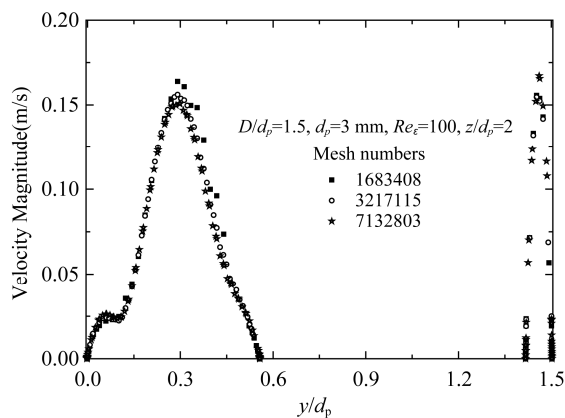


Fig. 4 Variations of velocity magnitude with mesh numbers in the packed bed with $D/d_p=1.5$.

Simulation Methodology

Simulations on flow and heat transfer in packed beds were carried out in ANSYS FLUENT 12.0. Three-dimensional Navier-Stokes equations, namely Eqs.(1–2), were firstly used to simulate the laminar flow of fluid through the packed bed. The one-equation turbulence equation, namely Eq.(5), was added for the turbulent flow. In this study, three interstitial Reynolds number Re_e of 10, 100 and 1000 were chosen to simulate the flow and heat transfer in packed beds. According to the transition regime of Dybbs and Edwards [15], the flow is laminar for $Re_e = 10$ and 100, and turbulent for $Re_e = 1000$. Air was chosen as

the fluid through the bed and its physical property parameters are: $\rho = 1.225 \text{ kg/m}^3$, $c_p = 1006 \text{ J/(kg} \cdot \text{K)}$, $k_f = 0.0242 \text{ W/(m} \cdot \text{K)}$ and $\mu = 1.78 \times 10^{-5} \text{ Pa} \cdot \text{s}$. The operation condition pressure is 101325Pa. Boundary conditions were set as velocity-inlet for inlet of packed bed, pressure-outlet for outlet of packed bed, no-slip wall condition for surface of particles and wall. The pressure-velocity coupling was carried out by the SIMPLE scheme. Second-order upwind schemes were used for the convective terms in the momentum equation. Simulations were not stopped until the residuals fall below 1×10^{-5} for density, velocity and turbulent kinetic energy. Moreover, the drag in the surface of particles was as a monitor for simulations of flow. Then the predicted flow results were used to simulate fluid-to-wall heat transfer by solving the energy equation, namely Eq.(3). Boundary conditions were set as 373K for inlet of packed bed, heat insulation for surface of particles, and 293.15K for tube wall. Second-order upwind schemes were used for the convective terms in the energy equation. Simulations were not stopped until the residuals fall below 1×10^{-9} for energy. The average temperature in the surface of particles was also as a monitor for simulations of heat transfer.

Validation

To validate the reliability of CFD simulation on packed beds, the CFD results of pressure drop were compared with the predicted values by correlations of Ergun [16], Zhavoronkov et al. [17] and Reichelt [18], as shown in Fig. 5. It can be seen that the simulated results are in good agreement with those estimated using Zhavoronkov et al.'s and Reichelt's correlations for $Re_e = 10$ and 100. The pressure drop in packed beds with small D/d_p is underestimated by Ergun's equation at low Reynolds number due to wall friction or viscous forces effects at the wall. The simulated results are slightly greater than those estimated by correlations for $Re_e = 1000$, which may be caused by the entrance effect and global shrinking of particles. What also can be seen from Fig. 5 is that pressure drop per unit length increases with the increasing of

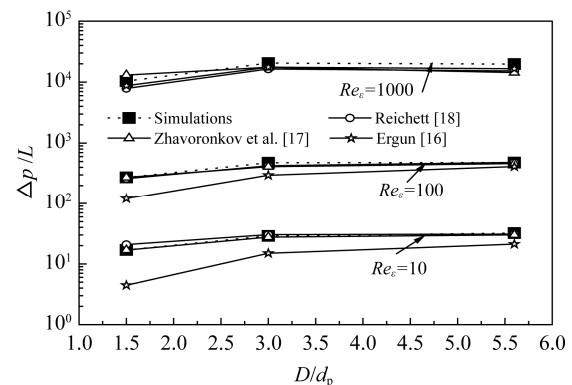


Fig. 5 Comparison of values of pressure drop between CFD calculation and prediction of correlations.

tube-to-particle diameter ratio due to the decreasing of void fraction. However, the increasing rate of it decreases with the increasing of tube-to-particle diameter ratio possibly on the account that the decreasing rate of void fraction also does.

Results and Discussion

Local fluid-to-wall heat transfer coefficient

Local fluid-to-wall heat transfer coefficient could be obtained through dividing temperature difference between the average temperature of fluid and wall temperature in infinitesimal cylinder by the heat rate transferred through the wall between z and $z+dz$. The calculating equation could be expressed as follows:

$$h_z = \frac{q_w|_{dz}}{T_{f,ave}|_{dz} - T_w} \quad (7)$$

Fig. 6 shows the distributions of fluid-to-wall heat transfer coefficient and void fraction along the bed at different Reynolds number for various D/d_p . Local void fraction ε_z in infinitesimal cylinder between z and $z+dz$ could be obtained using the following equation:

$$\varepsilon_z = \frac{V_{p,dz}}{V_{dz}} \quad (8)$$

What can be seen from Fig. 6 are as follows: i) fluid-to-wall heat transfer coefficient is periodic oscillating along the bed with wave crest and trough alternately presenting. The fluid-to-wall heat transfer coefficient attains to the maximum at the inlet of the bed, then quickly decreases, and finally becomes periodic oscillating.

The distribution of fluid-to-wall heat transfer coefficient along the bed is similar to that of local void fraction, just with their wave crest and trough in different positions. In packed beds with same D/d_p , local fluid-to-wall heat transfer coefficient increases with the increasing of interstice Reynolds number, as well as difference value between peak and trough adjacent. And, the positions of wave trough in the distributing curve move to the outlet direction of the bed with the increasing of Re_e . Under the condition of equivalent interstice Reynolds number Re_e , local fluid-to-wall heat transfer coefficients decrease with the increasing of tube-to-particle diameter ratio D/d_p , as well as different values between peak and trough adjacent, which may be dependent on the decrease of oscillation in void fraction near the wall. The three rules above will be explained in detail using field synergy principle in the next section.

Fig. 7 shows temperature contour maps in the x - z plane for different D/d_p at $Re_e=100$. It can be seen that periodic thermal boundary layers present near the wall, which further confirms the existence of the oscillation of wall heat transfer coefficient along the bed. In addition, it also can be found that the temperature gradient in the region away from the wall is much less than that near the

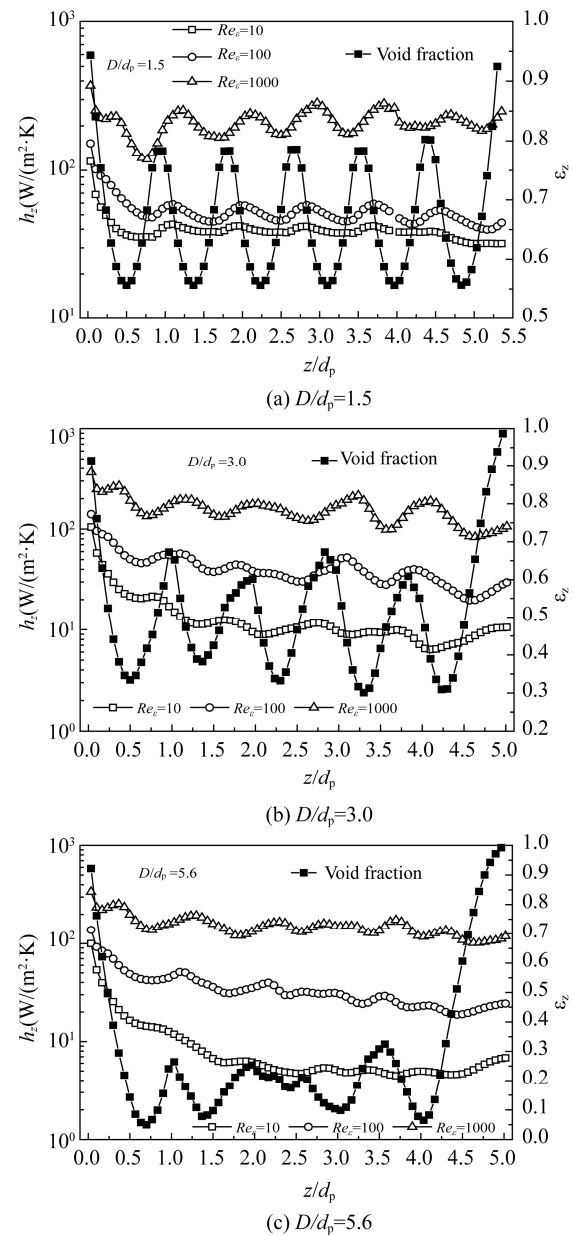


Fig. 6 Local fluid-to-wall heat transfer coefficients along the bed at different Reynolds number and local void fraction along the bed

wall for the cases studied. It elucidates that the mixing heat resistance in the region away from the wall is much less than the heat resistance near the wall for the cases studied. In other words, the periodically oscillating behavior of fluid-to-wall heat transfer coefficient along the bed is, to a great extent, from the periodical change of void fraction near the wall. The reason why the oscillating characteristic of heat transfer coefficient along the bed cannot be obtained in theoretical models may be that void fraction is set to constant in the model, but void fraction, especially near the wall, is oscillating along the bed with small tube-to-particle diameter ratio.

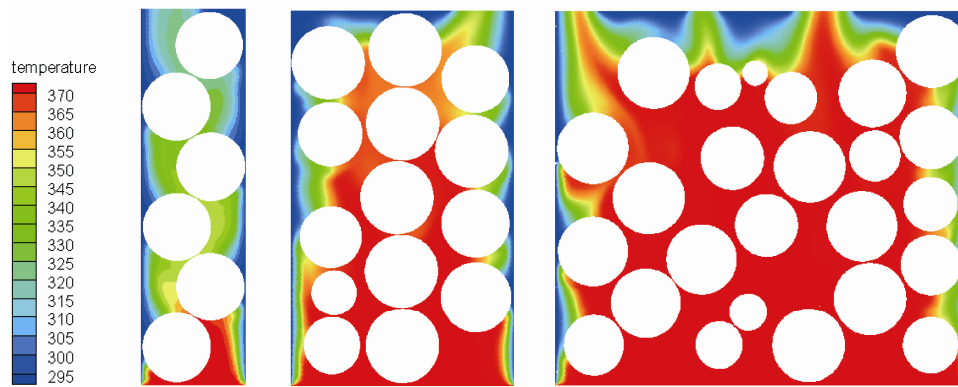


Fig. 7 Temperature contour maps in the x - z plane for different tube-to-particle diameter ratio at $Re_c=100$.

Field synergy analysis

Field synergy principle, proposed by Guo and Li [19], elaborates the physical mechanism of convection heat transfer in the view of the synergy between flow field and temperature field. This theory demonstrates that the performance of convection heat transfer depends not only on the velocity of fluid, the physical properties and the temperature difference between fluid and wall, but also on the synergy angle of velocity field and temperature field. In other words, the better the synergy between velocity and temperature fields is, the higher is the intensity of heat transfer under the same boundary conditions of velocity and temperature.

It can be concluded from the previous section that there are some relationship between the oscillation of fluid-to-wall heat transfer coefficient along the bed and the distributions of local void fraction and local packing structure. However, how void fraction and packing structure affect fluid-to-wall heat transfer still needs to be further accounted for by field synergy principle. In numerical simulations, the synergy angle θ_i in a mesh element between velocity and temperature gradient can be calculated from Guo and Huang [20]:

$$\theta_i = \arccos \left(\frac{\vec{U} \cdot \nabla T}{|\vec{U}| |\nabla T|} \right) \quad (10)$$

The local average synergy angle $\theta_{ave,z}$ in the x - y plane in the position of z , can be acquired from Guo and Huang, [20]:

$$\theta_{ave,z} = \frac{\sum_z A_i \theta_i}{\sum_z A_i} \quad (11)$$

Fig. 8 shows the distributions of fluid-to-wall heat transfer coefficient h_z and local average synergy angle $\theta_{ave,z}$ along the bed. It can be seen from Fig. 8 that synergy angle at the inlet attains to the minimum, and thus the synergistic characteristics there is the best throughout the

bed leading to the strongest intensity of heat transfer. Then the synergy presents a periodically oscillating characteristic, so does the corresponding heat transfer coefficient. This may be caused by the periodic variation of local void fraction near the wall.

Fig. 9 shows the distributions of velocity and temperature in the x - y plane for $D/d_p=1.5$ at different Reynolds number. It also can be seen that the synergistic characteristic at the inlet is the best throughout the bed, and the synergy as well as the arrangement structure of particles presents a periodicity along the bed. Typically, a triangular structure formed by three particles and wall (Zone 1), periodically presents along the bed, as shown in Fig. 9. In this triangular structure, the synergy is good at the corner between two particles close to the entrance of the bed, whereas a bit poor at other place. It is consistent with the distribution of local average synergy angle along the bed in Fig. 8.

The other phenomenon, observed from Fig. 9, is that eddy appears if interstice Reynolds number attains to 100, which is in favor of the synergy enhancement. The heat transfer intensity is directly proportional to flow velocity. Local heat transfer coefficients therefore increase with the increasing of flow velocity. Moreover, the oscillating amplitude of the distributing curve of local heat transfer coefficients increases with the increasing of flow velocity. This is because the heat transfer is significantly enhanced in the location of small synergy angle with the increasing of flow velocity, whereas that in the location of large synergy angle changes little.

The synergy characteristics in packed beds with $D/d_p=3.0$ and $D/d_p=5.6$ has the same distributions as in the packed bed with $D/d_p=1.5$, as well as the influence mechanism of flow velocity on heat transfer, as shown in Figs.10–13. Just the local average synergy angle increases with the increasing of tube-to-particle diameter ratio at the equivalent interstice Reynolds number.

The decrease of synergy characteristics with the increasing of tube-to-particle diameter ratio may be due to

the fact that the amount of the triangular structure formed by three particles and the wall like Zone 1 in Figs. 9, 11 and 13 reduces near the wall with the increase of D/d_p . This causes the decrease of values and axial oscillating amplitude of local heat transfer coefficients. Based on this rule, we can predict that the oscillating behavior of heat transfer coefficient along the bed will disappear only if tube-to-particle diameter ratio is large to an extent since the uniformity of void fraction prevails near the wall in the axial direction of the bed. In Figs. 11 and 13, the triangular structure can be observed in a little place near the wall, and eddy also appears if flow velocity reaches a specific value. In fact, the synergy between velocity field and temperature field formed in this triangular structure, on the whole, is the best among all struc-

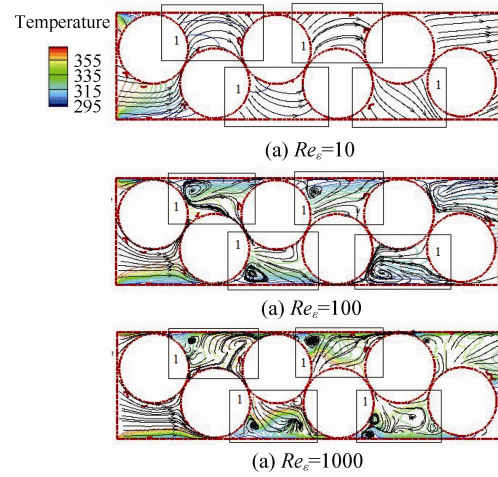


Fig. 9 Streamline and temperature contours in the x - z plane in the packed bed with $D/d_p=1.5$.

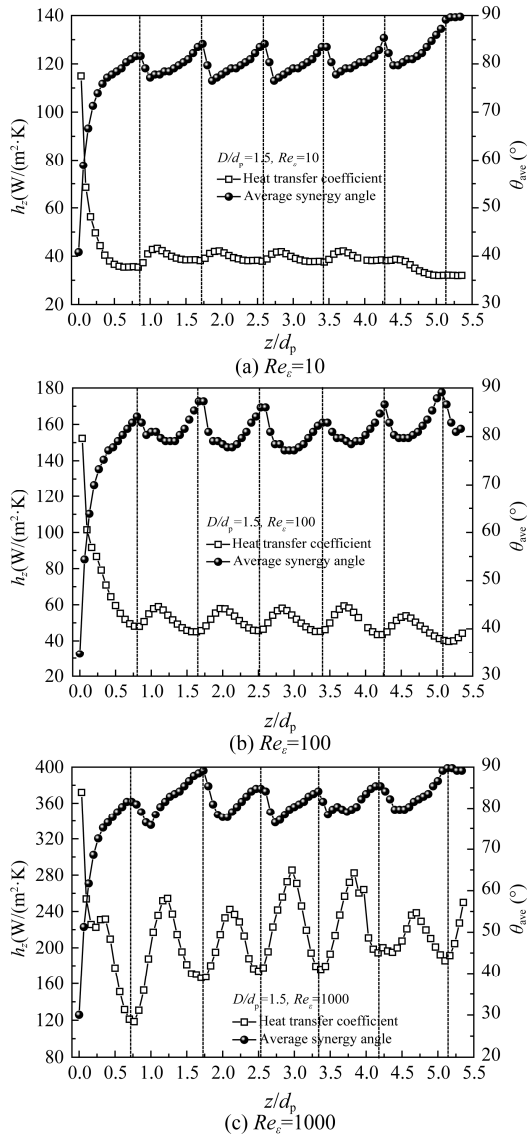


Fig. 8 Local fluid-to-wall heat transfer coefficients and average synergy angle along the bed for $D/d_p=1.5$.

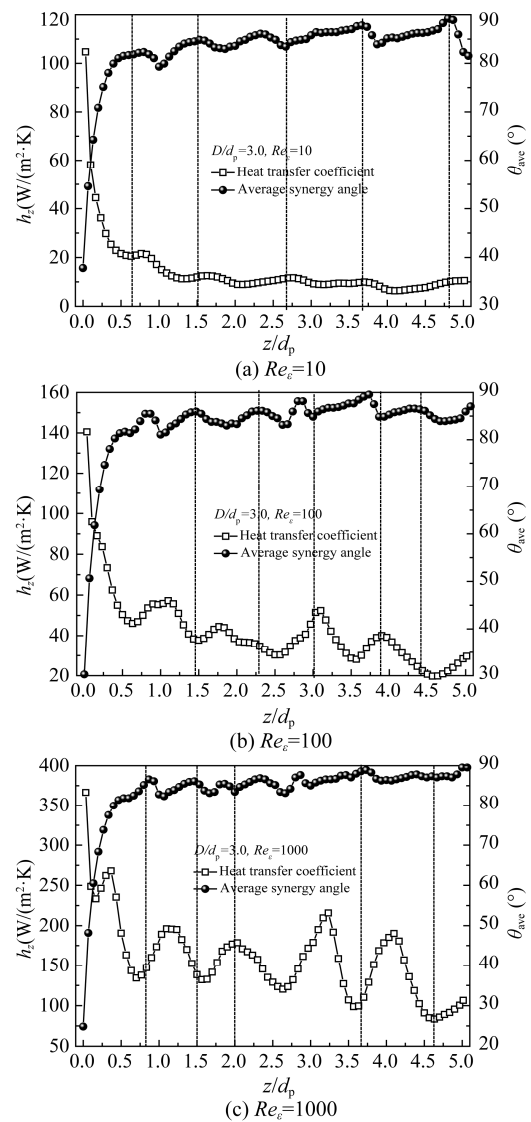


Fig. 10 Local fluid-to-wall heat transfer coefficients and average synergy angle along the bed for $D/d_p=3.0$.

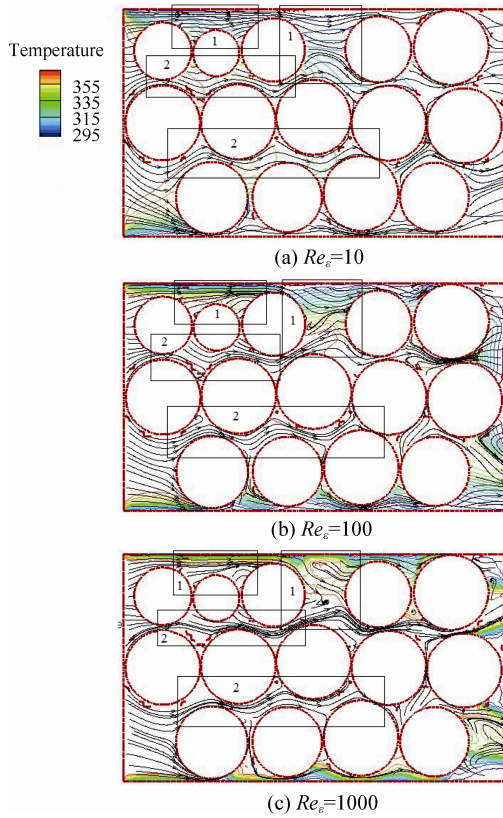


Fig. 11 Streamline and temperature contours in the x - z plane in the packed bed with $D/d_p=3.0$.

tures near the wall. Therefore, the triangle structure is suggested to be arranged near the wall as far as possible.

Based on the reinforcement mechanism of heat transfer, the synergy between velocity field and temperature field is good at the place where the disturbed flow forms (Yang and Tao [21]). In a randomly packed bed, the disturbed flow forming in two kinds of structures is strong in the region away from the wall: one is the rhombus structure with a pair of edges having a gap and another pair of edges not doing, like Zone 2 in Figs. 11 and 13, where the continuously disturbed flow may form; another is the rhombus structure with both two pairs of edges having a gap, like Zone 3 in Fig. 13, where the cross disturbed flow may form. The mixing of fluid is enhanced, and a jet may produce if the fluid flows through these two structures. Based on the existing theory, the cross disturbed flow is the best way to strengthen heat transfer among these two kinds of disturbed flows (Yang and Tao [21]). Therefore, the rhombus structure with both two pairs of edges having a gap is suggested to be arranged in the region away from the wall as far as possible.

To validate the reliability of the study on heat transfer in packed beds, the average wall Nusselt number obtained using Eq.(9) in the simulations are compared with predicted values of correlations suitable for the cases

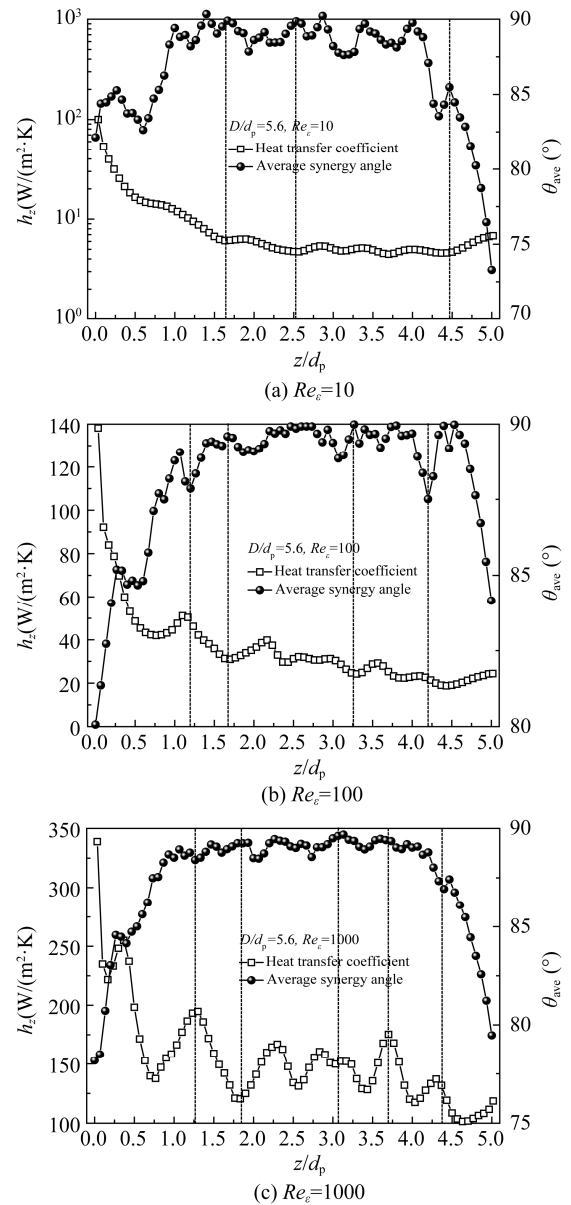


Fig. 12 Local fluid-to-wall heat transfer coefficients and average synergy angle along the bed for $D/d_p=5.6$.

studied, as shown in Fig. 14. It can be seen that CFD data are in good agreement with predicted values of correlations shown in Tab. 2 with deviation within 25%.

$$Nu_w = \frac{d_p}{k_f L} \int_0^L h_{w,z} dz \quad (9)$$

Conclusions

To understand fluid-to-wall heat transfer coefficient in packed beds, in this study, we firstly built randomly packing structure of particles in packed beds with small tube-to-particle diameter ratio ($D/d_p < 10$) using DEM, and then

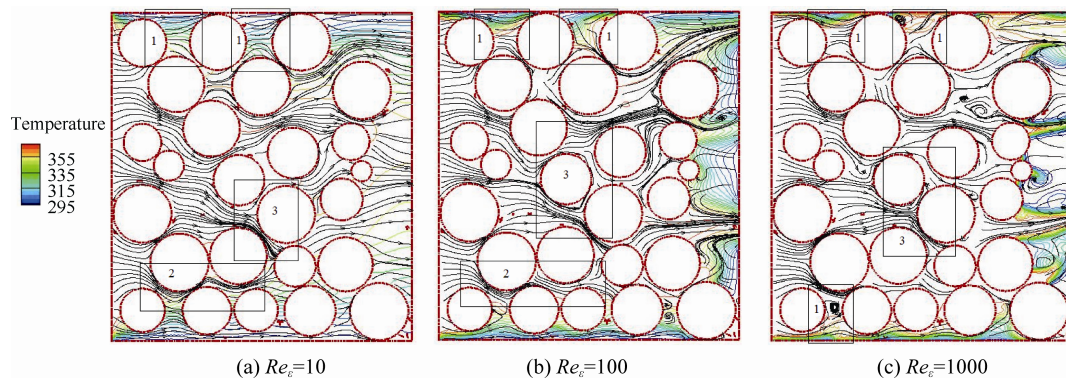


Fig. 13 Streamline and temperature contours in the x - z plane in the packed bed with $D/d_p=5.6$.

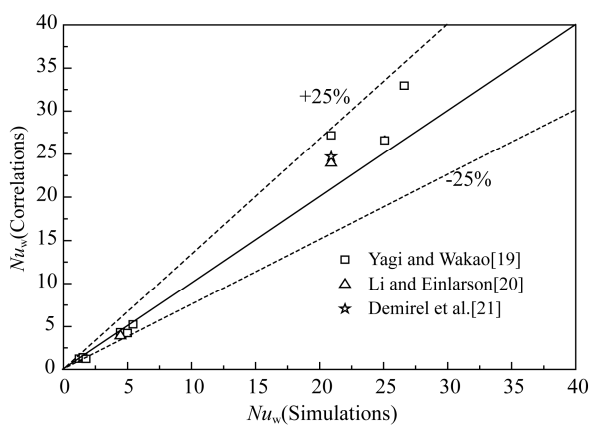


Fig. 14 Comparisons of average wall heat transfer coefficients between the simulations and the correlations.

simulated the fluid-to-wall heat transfer by CFD. Finally, we demonstrated the characteristics of local fluid-to-wall heat transfer and its relationship with local structure and flow using field synergy principle. The following major conclusions can be drawn.

(1) In packed beds with small D/d_p , the fluid-to-wall heat transfer coefficient is periodically oscillating along the bed with wave crest and trough alternately presenting. It attains to the maximum at the inlet of the bed, then quickly decreases, and finally becomes a periodical oscillating. The distributions of fluid-to-wall heat transfer coefficient along the bed are similar to that of local void fraction, just with their wave crest in different positions;

(2) In packed beds with same D/d_p , the fluid-to-wall heat transfer coefficient increases with the increasing of interstice Reynolds number Re_e , as well as difference values between peak and trough adjacent;

(3) Under the equivalent interstice Reynolds number, the fluid-to-wall heat transfer coefficient decreases with the increasing of tube-to-particle diameter ratio D/d_p , as well as difference values between peak and trough adjacent. Based on this rule, we predict that the oscillating behavior of the local heat transfer coefficient along the

bed will disappear only if tube-to-particle diameter ratio is large to an extent since the uniformity of void fraction near the wall prevails along the beds;

(4) The distribution of fluid-to-wall heat transfer coefficient along the bed and the changing rules of it with flow velocity and tube-to-particle diameter ratio are elucidated through field synergy analysis on velocity and temperature fields. The triangular structure formed by three particles and the wall is suggested to be arranged near the wall and the rhombus structure with both two pairs of edges having a gap is suggested to be arranged in the region away from the wall.

Acknowledgements

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